

*Higher-order resonances in **single**-arm nanoantennas:  
Evidence of **Fano**-like interference  
FANO PLASMONICS MADE SIMPLE*

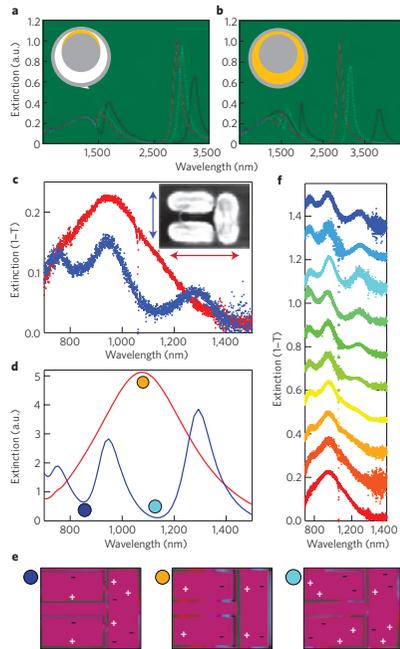
**F. López-Tejeira, R. Paniagua-Domínguez, R. Rodríguez-Oliveros**

**José A. Sánchez-Gil,**

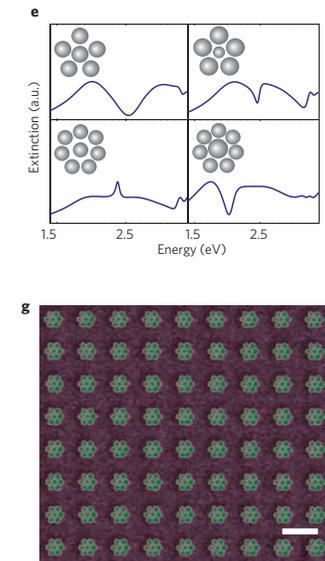
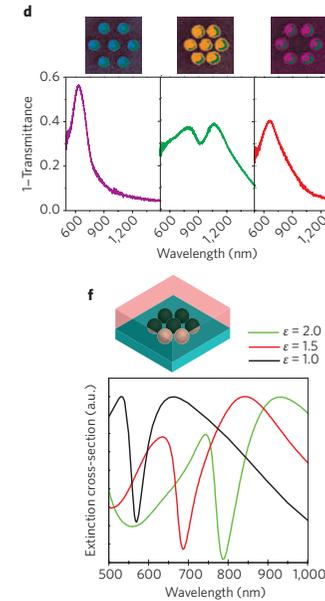
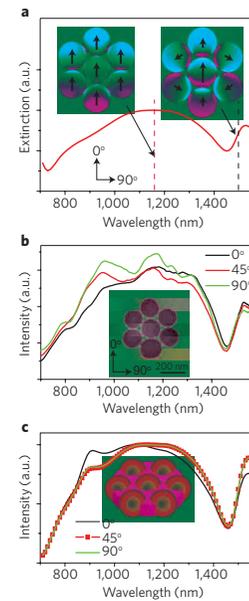
*Instituto de Estructura de la Materia (CSIC), Madrid (Spain)*

*Email: [j.sanchez@csic.es](mailto:j.sanchez@csic.es)*

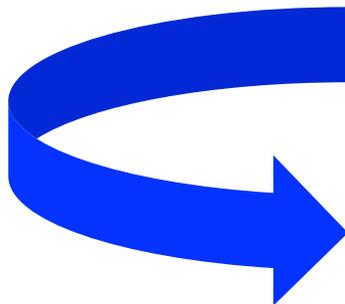
## Fano-like plasmon resonances on a variety of complex nanostructures



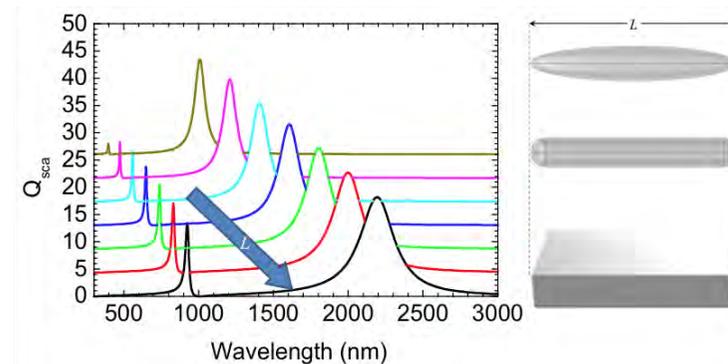
Nano-disk-rings,  
nanodolmens,  
nanoclusters, ...



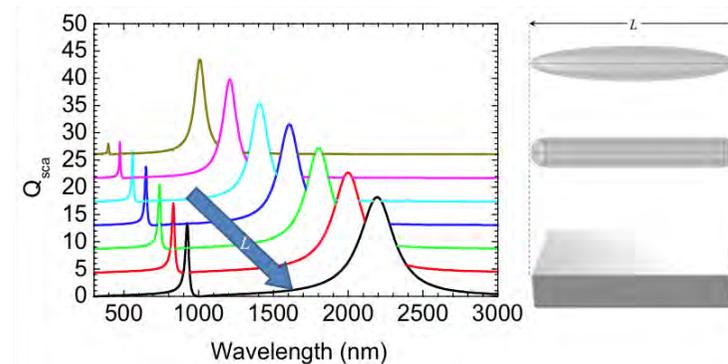
Luk'yanchuk, Zheludev, Maier, Halas, Nordlander, Giessen, Chong, Nat. Mater. 2010



- Introduction: Plasmon Fano reso/single-NP
- Nano-Spheroid
  - Quasi-analytical approach: Mode interference
- Nano-rods & nano-wires
  - Numerical calcs
  - 1<sup>st</sup>-3<sup>rd</sup> mode: Spatial interference
- Conclusions:  
Spectral & spatial overlap



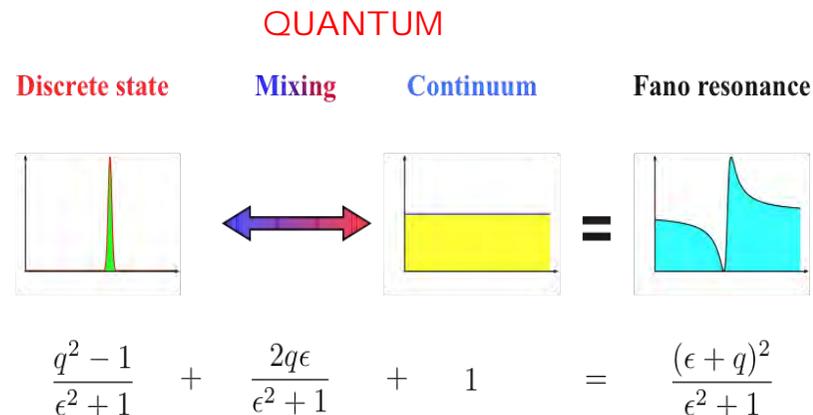
- Introduction: Plasmon Fano reso/single-NP **Why not?**
- Nano-Spheroids
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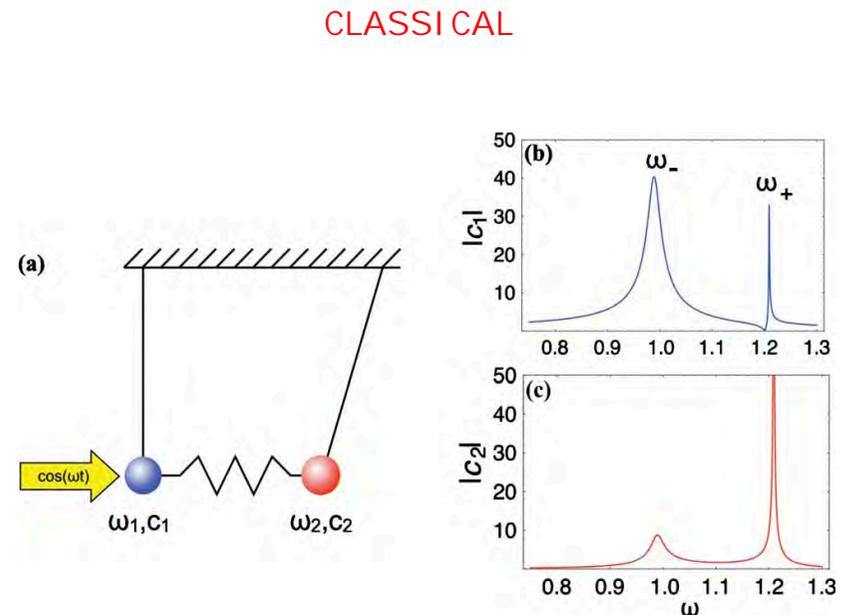
A **Fano resonance** exhibits a distinctly asymmetric shape with the following functional form:

$$\frac{(F\gamma + \omega - \omega_0)^2}{(\omega - \omega_0)^2 + \gamma^2}$$

where  $\omega_0$  and  $\gamma$  are standard parameters that denote the position and width of the resonance, respectively;  $F$  is the so-called Fano parameter, which describes the degree of asymmetry. The microscopic origin of the Fano resonance arises from the constructive and destructive interference of a narrow discrete resonance with a broad spectral line or continuum.



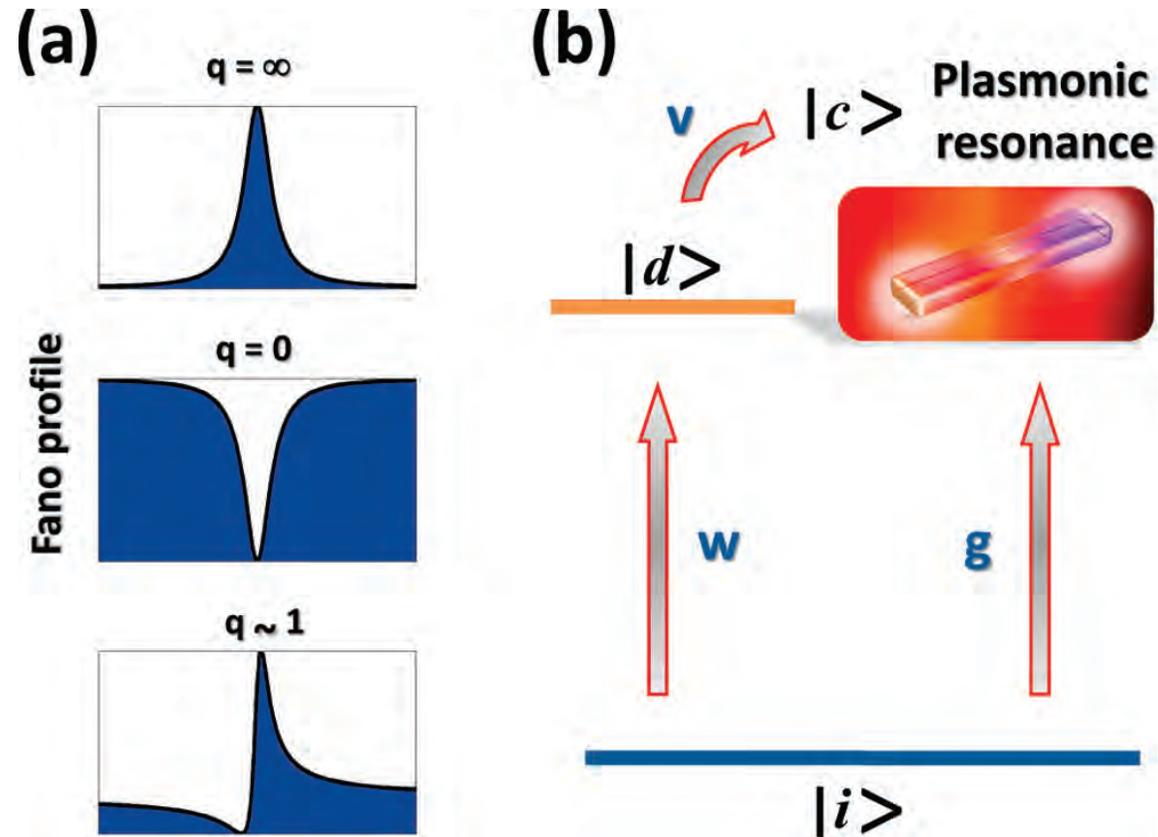
Fano, "Effects of configuration interaction on intensities and phase shifts", Phys. Rev. 1961.



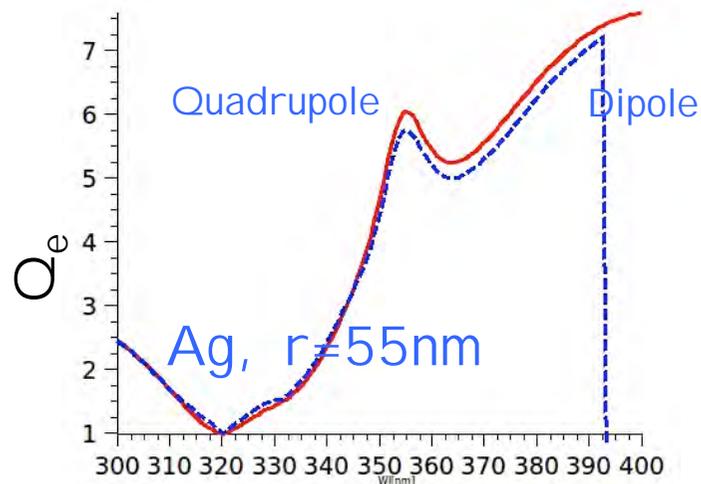
Joe, Satanin, and Kim, "Classical analogy of Fano resonances," Phys. Scr. 2006.

## Plasmon-Fano model

Giannini, Francescato, Amrania, Phillips, Maier, Nano Lett. 2011



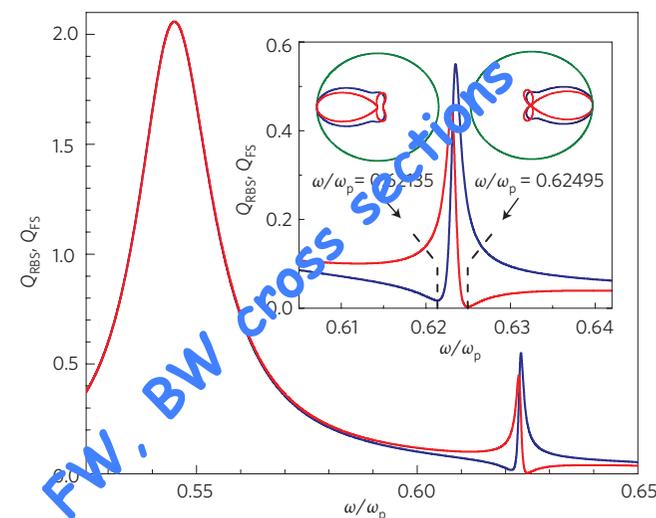
## PLASMONICS: SPHERE → Mie scattering



BROAD mode (Lowest-order, E-Dipole)  
DARK mode (Higher-order, EM Multipole)

$$Q_{sca} = \frac{2}{q^2} \sum_n (2n + 1) \left[ |a_n|^2 + |b_n|^2 \right]$$

$Q_{sca}$  Mie → NO INTERFERENCE!!

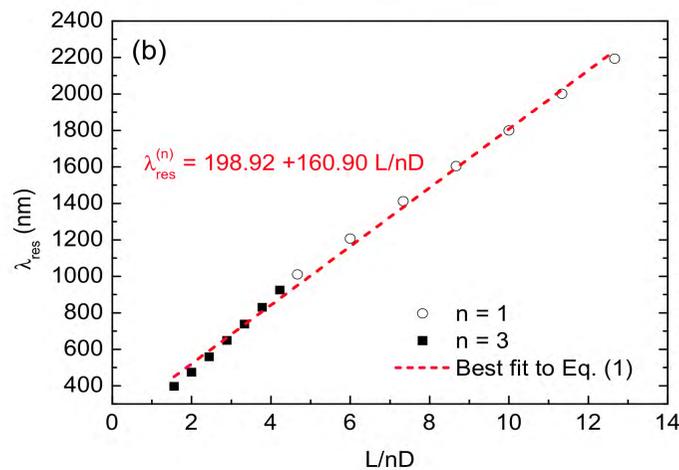
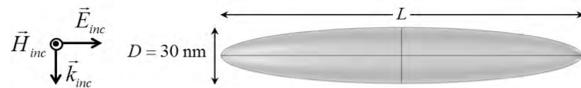
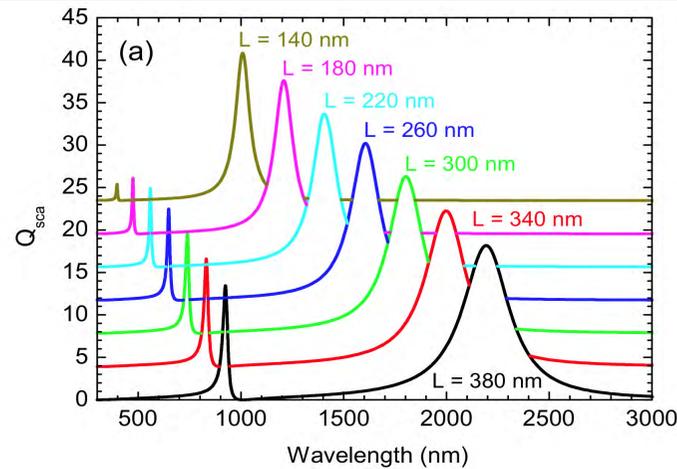


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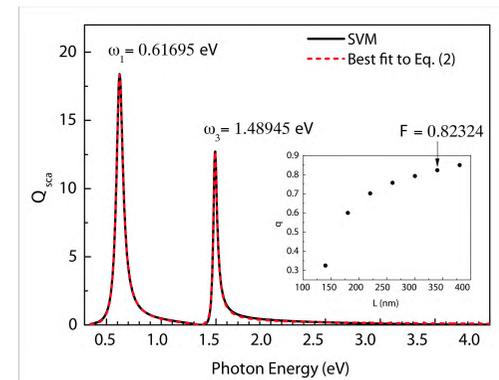
## Longitudinal plasmon resonances Separation of variables (SVM)

Normal incidence: odd-symmetry modes



## Modified Fano line shape

$$Q_{sca}(\omega) \propto \left| A(\omega) + B \left[ \frac{b_1}{(\omega - \omega_1) + ib_1} + \frac{Fb_3}{(\omega - \omega_3) + ib_3} \right] \right|^2$$

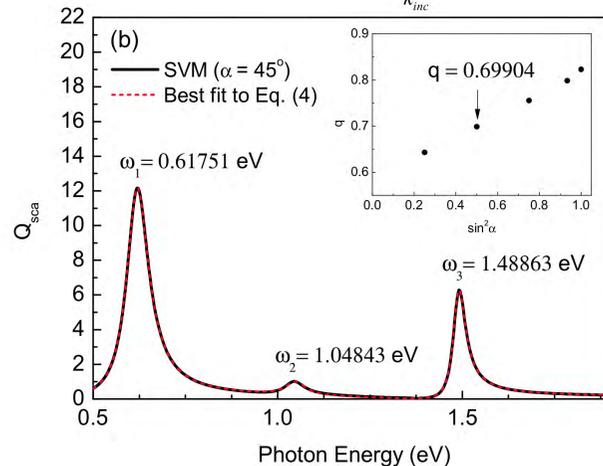
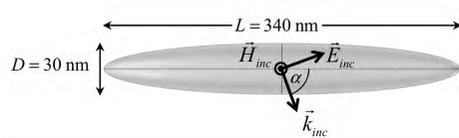
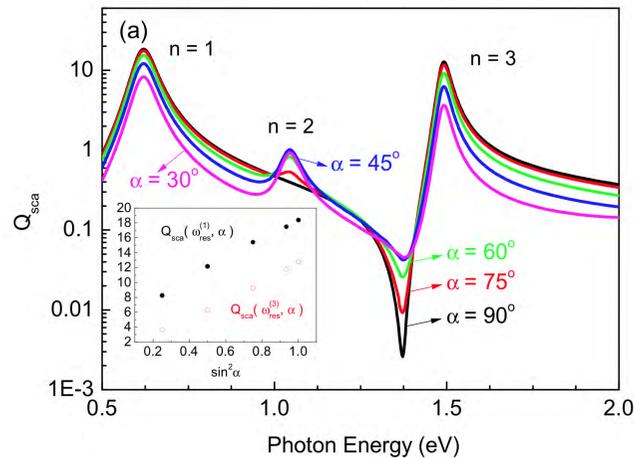


López-Tejera, Rodríguez-Oliveros, Paniagua-Domínguez, Sánchez-Gil, preprint

## Longitudinal plasmon resonances

Oblique incidence: all modes  $n=1,2,3,\dots$

SVM



Fano line-shape + Lorentzian  
 $N=1,3$  +  $N=2$



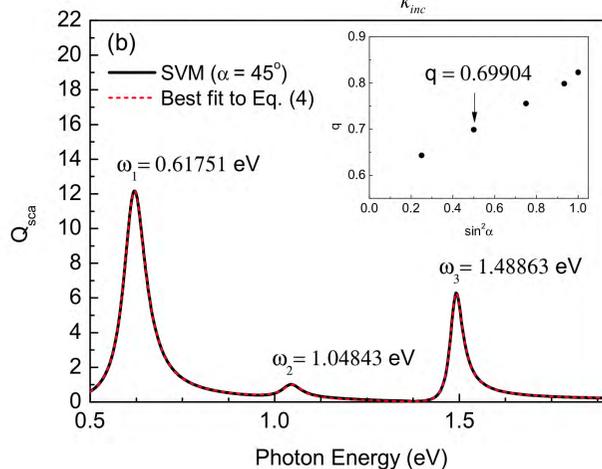
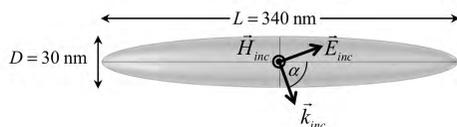
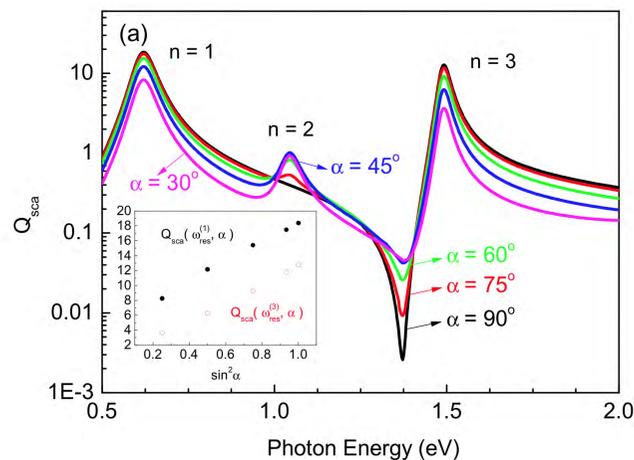
$$Q_{sca}(\omega, \alpha \neq 90^\circ) \approx |f(\omega)|^2 + \frac{|B_2|^2 b_2^2}{b_2^2 + (\omega - \omega_2)^2}$$

López-Tejiera, Rodríguez-Oliveros, Paniagua-Domínguez, Sánchez-Gil, preprint

## Longitudinal plasmon resonances

Oblique incidence: all modes  $n=1,2,3,\dots$

## Separation of variables (SVM) ~ Extended Mie



$$Q_{sca} = \frac{4}{LDk_d^2} \left\{ 2 \sum_{l=1}^{\infty} |b_l^{(1)}|^2 N_{1l}^2(c_d) + \text{Re} \sum_{l=1}^{\infty} \sum_{m=l}^{\infty} \sum_{n=m}^{\infty} i^{n-l} \left[ k_d^2 a_{ml}^{(d)} (a_{mn}^{(d)})^* \omega_{ln}^{(m)}(c_d, c_d) + ik_d \left( b_{ml}^{(d)} (a_{mn}^{(d)})^* \kappa_{ln}^{(m)}(c_d, c_d) - a_{ml}^{(d)} (b_{mn}^{(d)})^* \kappa_{nl}^{(m)}(c_d, c_d) \right) + b_{ml}^{(d)} (b_{mn}^{(d)})^* \tau_{ln}^{(m)}(c_d, c_d) \right] N_{ml}(c_d) N_{mn}(c_d) \right\}$$



Mie-like: NO INTERFERENCE

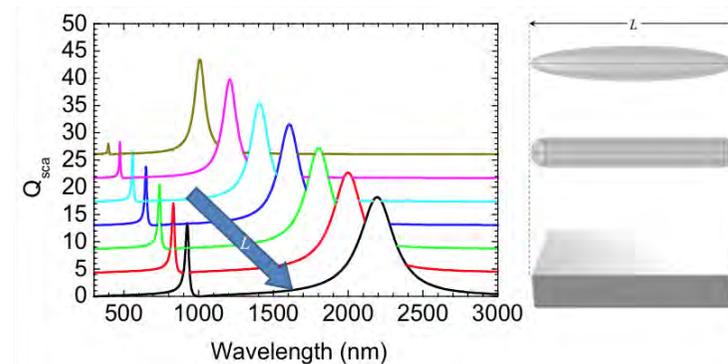


Ext-Mie: INTERFERENCE

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- Plasmon Fano reso/**single-Nano-Spheroids**
- Quasi-analytical approach: Mode interference
- Odd modes: 1<sup>st</sup>-3<sup>rd</sup> interference
- Even-odd modes: 1<sup>st</sup>-2<sup>nd</sup> NO interference
- Explore other single NP geometries

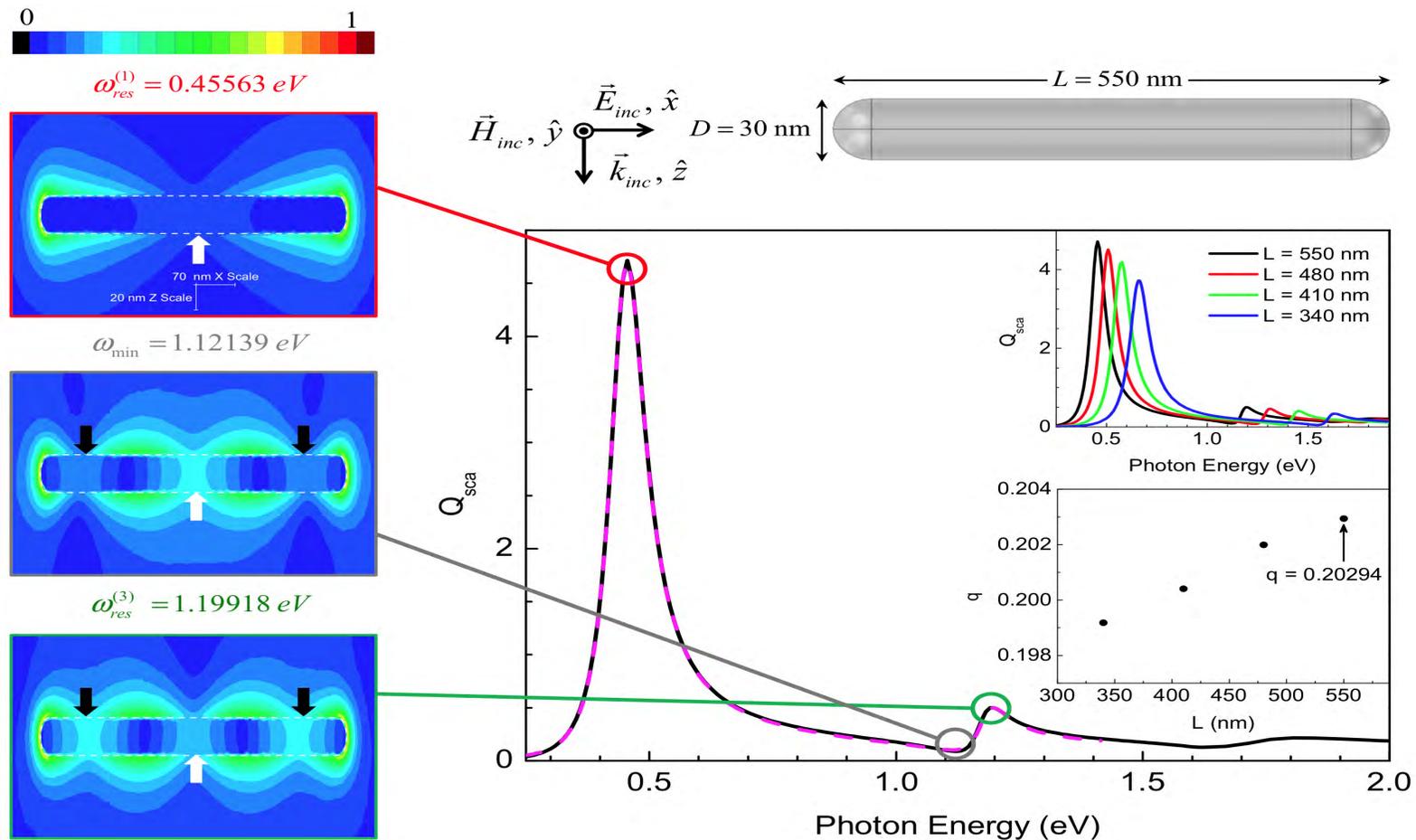
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## Longitudinal $L \sim n\lambda/2$ resonances

Oblique incidence: all modes  $n=1,2,3,\dots$

## FEM-COMSOL



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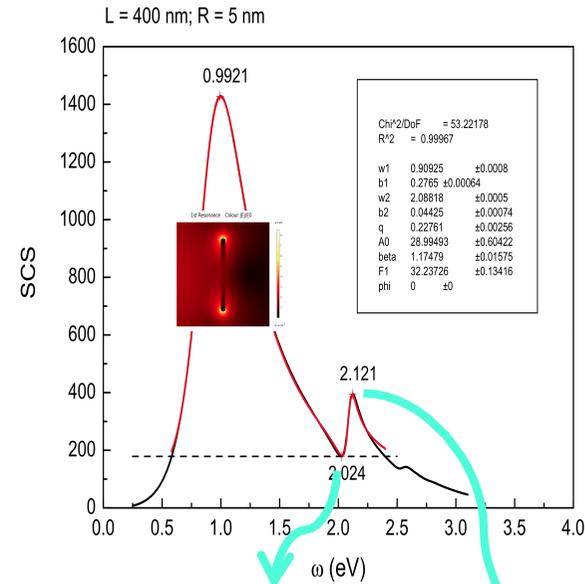
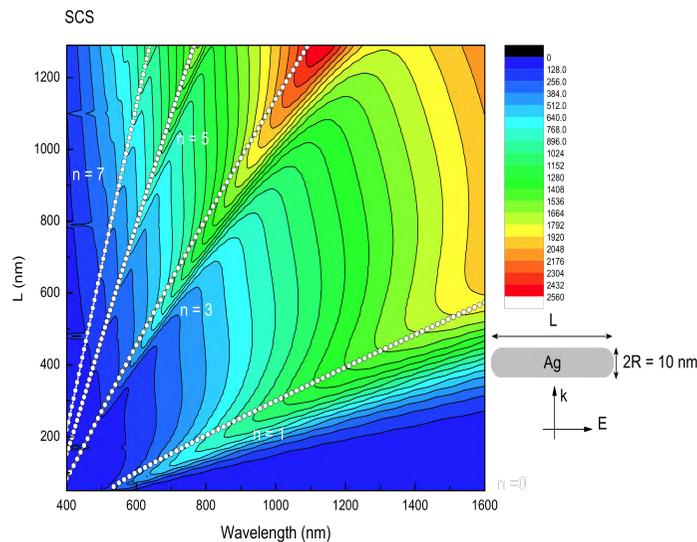
Nanowire (~2D Nanorods)

Longitudinal  $L = n\lambda_{\text{eff}}/2[1-R]$  resonances

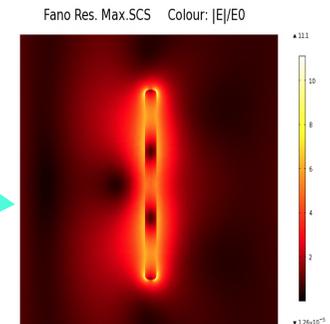
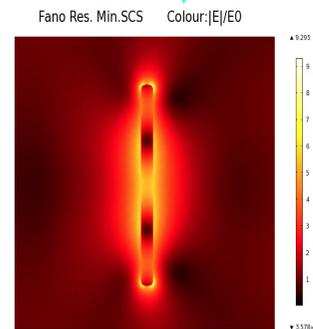
Normal incidence: odd modes

$n=1$  (HW) ▶ Broad, Bright  
 $n=3,5,\dots$  (HW) ▶ Narrow, Dark

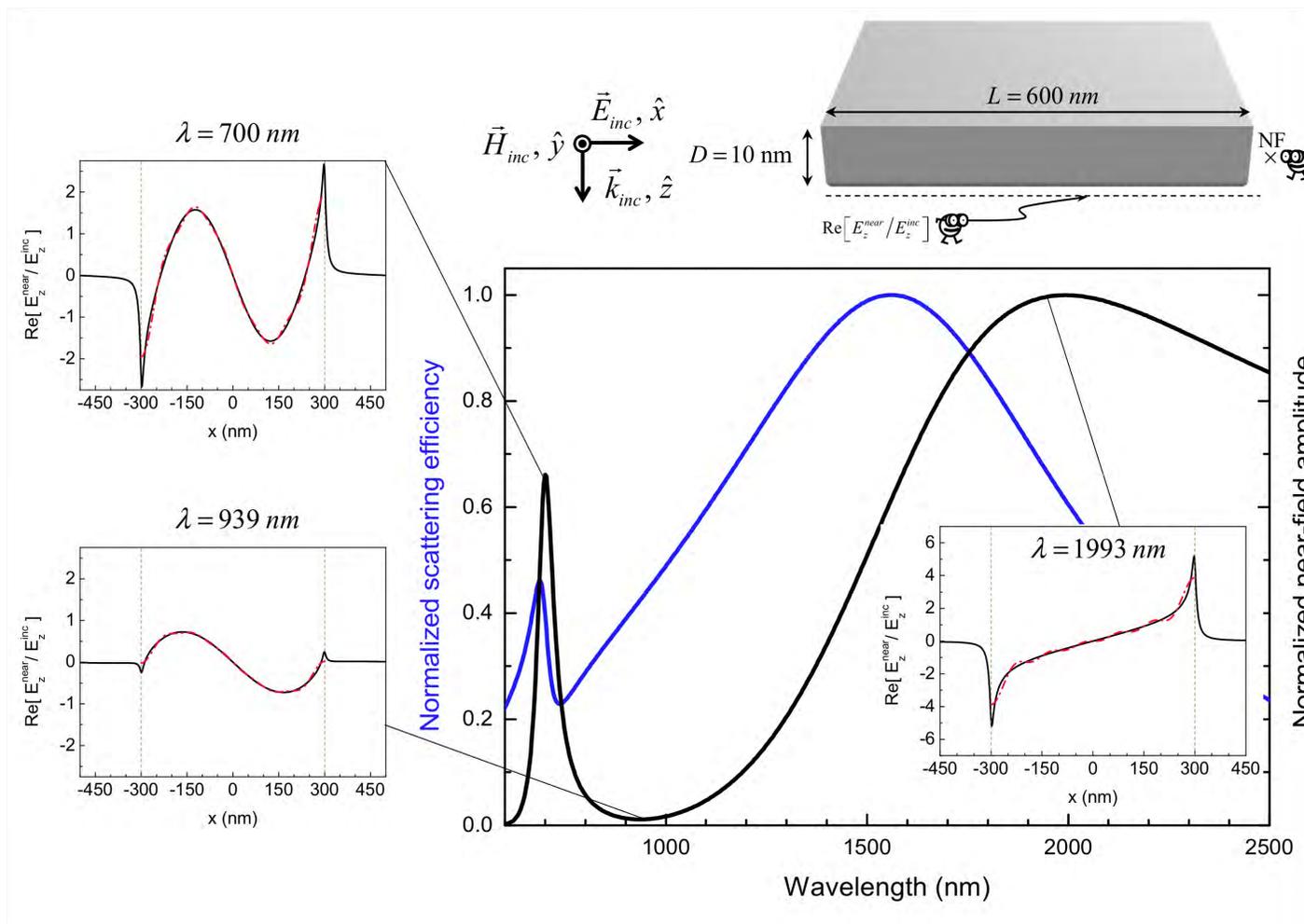
2DSIE



Modified Fano line-shape fit



## Spatial Mode Interference



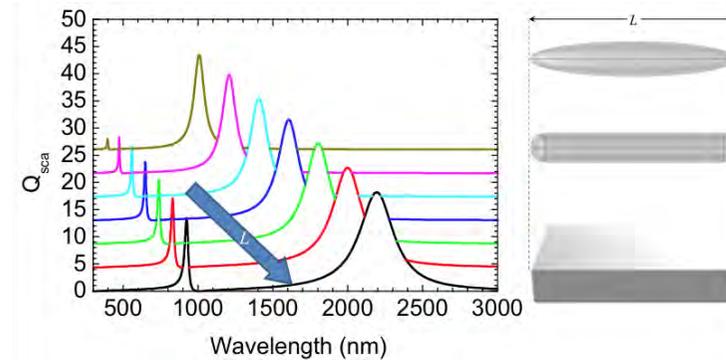
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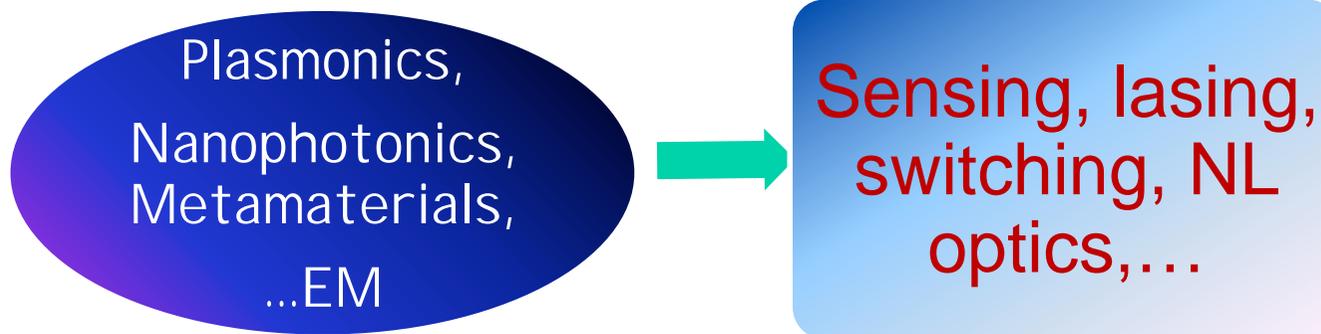
► Fano-like LSPR on a single nanorod

► Spectral & Spatial overlap

Explore new physics & configurations



► Applications: Fano made simple!!



## Coworkers

*Instituto de Estructura de la Materia (CSIC), Madrid (Spain)*



**Rogelio Rodríguez-Oliveros**

**Ramón Paniagua-Domínguez**



**Fernando López-Tejeira**



## Funding agencies





IEM



*...Thank you*